

Exercise Sheet 7

Assignment 7.1 Attribute Grammars

The following $LL(1)$ grammar implements the functionality of a pocket calculator. Every key of the calculator emits a token. The keys 0 to 9 emit the token `digit` and all other keys directly translate to the tokens `=`, `+`, `*`, `mw` (memory write), and `mr` (memory read).

rule	production	attribute system
1	$Start ::= Comp$	$v[0] := v[1] \quad m[1] := 0$
2	$Comp ::= Expr =$	$v[0] := v[1] \quad m[1] := m[0]$
3	$ Expr = Comp$	$v[0] := v[3] \quad m[1] := m[0] \quad m[3] := m[0]$
4	$ Expr mw Comp$	
5	$Expr ::= Term + Expr$	
6	$ Term$	
7	$Term ::= Atom * Term$	
8	$ Atom$	
9	$Atom ::= digit Number$	
10	$ mr$	
11	$Number ::= digit Number$	
12	$ \epsilon$	

The result is computed in the v attribute of $Start$. The key `=` is used to evaluate the expression and clears the input. The value of the internal memory is stored in the attribute m which is initially zero. The key `mw` evaluates the expression and stores its value in the internal memory of the calculator, and clears the input. The key `mr` recalls this value. For each token `digit` the attribute v contains the digit as the natural number, i.e., $v \in [0, 9]$.

1. What is the result after parsing the following key strokes. For a parse error, write "err".

-
-
-
-
-

2. Complete the definitions for the result value v and the content of the memory cell m so that the calculator has the described behavior. You may add other attributes as needed.

3. Which properties does the attributed grammar satisfy?

- it is l-attributed
- v is inherited
- v is synthesized
- m is inherited
- m is synthesized
- it is acyclic

Assignment 7.2 Strongly Acyclic Attribute Grammars

Consider Attribute Grammar G :

$$\begin{array}{lcl}
 S' & \rightarrow & A^0 \\
 A & \rightarrow & s B^0 \\
 & | & t B^1 \\
 B & \rightarrow & u^0 \\
 & | & v^1
 \end{array}
 \left|
 \begin{array}{l}
 z[0] := z[1] \quad c[1] := 0 \\
 a[2] := y[2] \quad b[2] := c[0] \quad z[0] := x[2] \\
 a[2] := c[0] \quad b[2] := x[2] \quad z[0] := y[2] \\
 x[0] := a[0] \quad y[0] := b[0] \\
 y[0] := x[0] \quad x[0] := 0
 \end{array}
 \right.$$

1. Draw the local dependency graphs for all production rules $p \in G$.
2. Enumerate all inputs and construct the dependency graphs.
3. Is G acyclic?