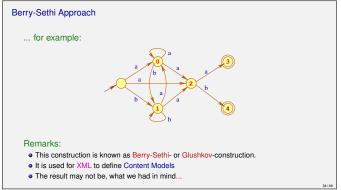


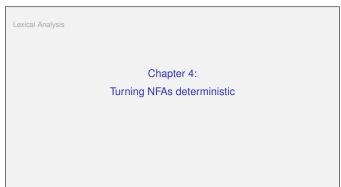
```
Berry-Sethi Approach: (sophisticated version)

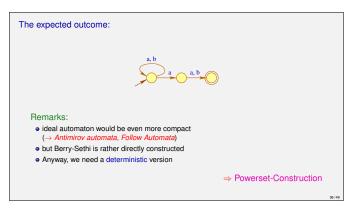
Construction (sophisticated version):
Create an automaton based on the syntax tree's new attributes:

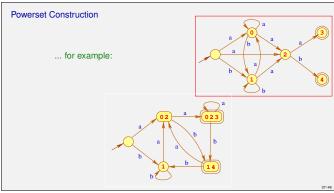
States: \{\bullet e\} \cup \{i \bullet \mid i \text{ a leaf not } e\}
Start state: \bullet e

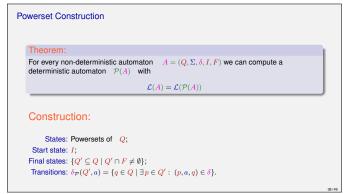
Final states: last[e] if e if e
```

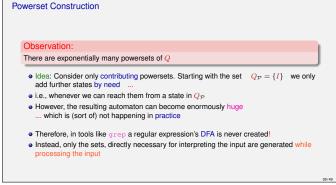


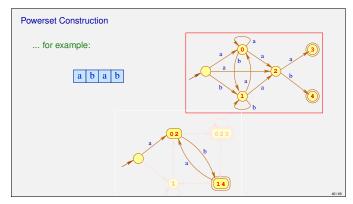


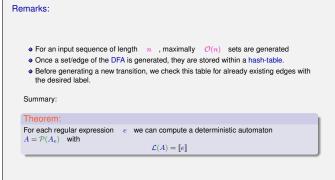


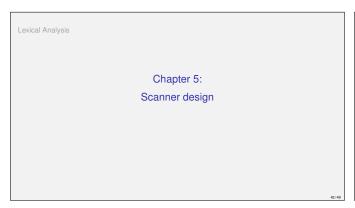




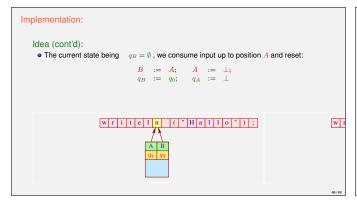








```
Scanner design \begin{array}{ll} & & \\ & e_1 & \left\{ \begin{array}{c} \text{action}_1 \\ e_2 & \left\{ \text{action}_2 \right\} \\ & \dots \\ & e_k & \left\{ \begin{array}{c} \text{action}_k \end{array} \right\} \end{array} \\ & \text{Output:} & \text{a program,} \\ & \dots & \text{reading a maximal prefix } w \text{ from the input, that satisfies } e_1 \mid \dots \mid e_k; \\ & \dots & \text{determining the minimal} \quad i \quad , \text{ such that } \quad w \in \llbracket e_i \rrbracket; \\ & \dots & \text{executing action}_i \text{ for } w. \end{array}
```

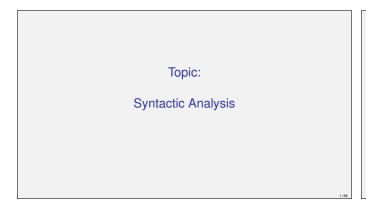


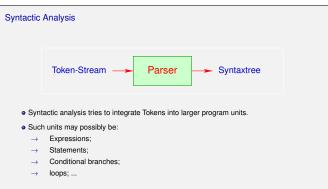
```
    Now and then, it is handy to differentiate between particular scanner states.
    In different states, we want to recognize different token classes with different precedences.
    Depending on the consumed input, the scanner state can be changed

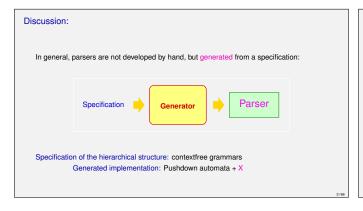
Example: Comments

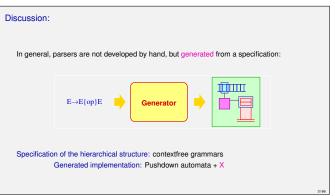
Within a comment, identifiers, constants, comments, ... are ignored
```

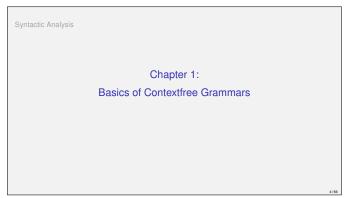
"." matches all characters different from "\n".
 For every state we generate the scanner respectively.
 Method yybegin (STATE); switches between different scanners.
 Comments might be directly implemented as (admittedly overly complex) token-class.
 Scanner-states are especially handy for implementing preprocessors, expanding special fragments in regular programs.



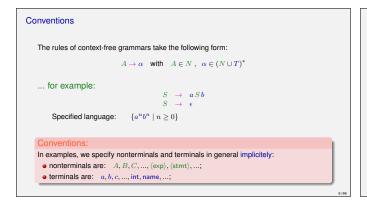


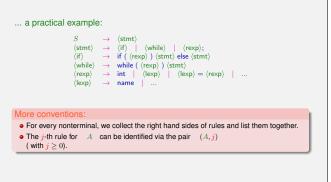


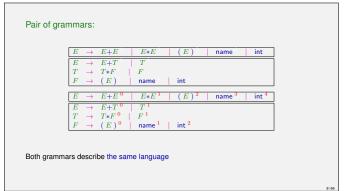


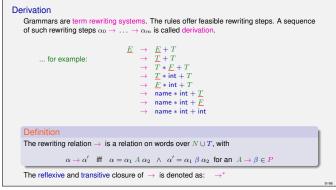


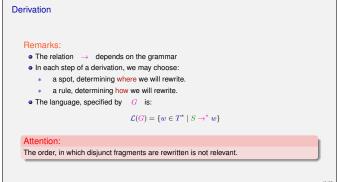


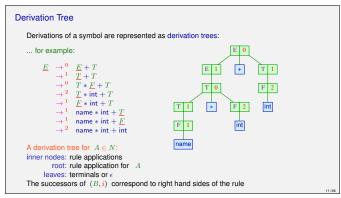


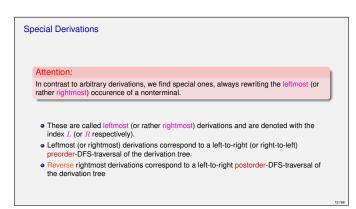


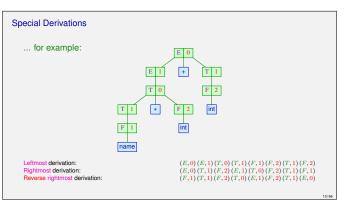


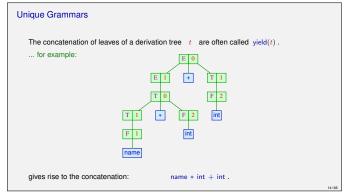


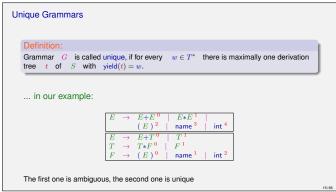


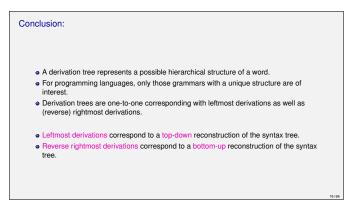


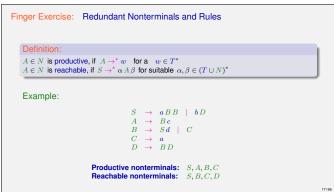


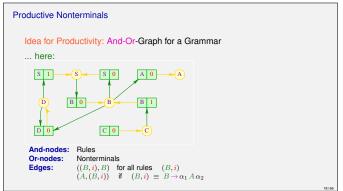


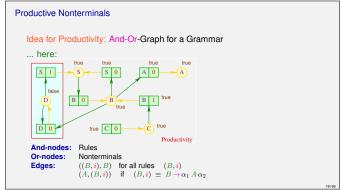


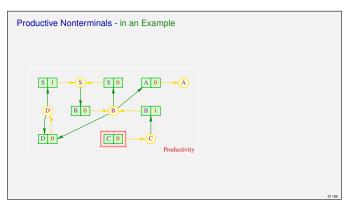


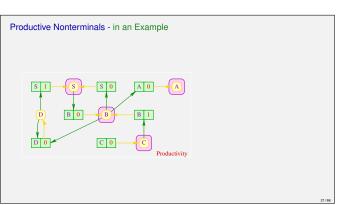












### Runtime:

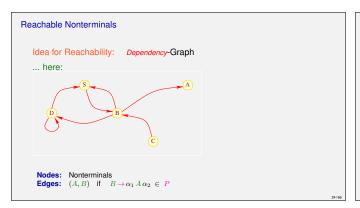
- Initialization of data structures is linear.
- ullet Each rules is added once to W at most.

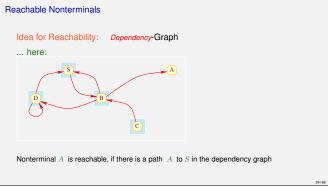
### Correctness:

- $\bullet$  If A is added to result in the j-th iteration of the **while**-loop there is a derivation tree for A of height maximally j
- ullet For every derivation tree the root is added once to W

Discussion:

- ullet To simplify the test  $(A \in \mathsf{result})$  , we represent the set  ${\mathsf{result}}$  as an  ${\mathsf{array}}$ .
- ullet W as well as the sets  $\operatorname{rhs}[A]$  are represented as Lists
- The algorithm also works for finding smallest solutions for Boolean inequality systems
- $\mathcal{L}(G) \neq \emptyset$  (  $\rightarrow$  *Emptyness Problem*) can be reduced to determining productive nonterminals





### **Reduced Grammars**

### Conclusion:

- Reachability in directed graphs can be computed via DFS in linear time.
- This means the set of all reachable and productive nonterminals can be computed in

A Grammar G is called reduced, if all of G's nonterminals are productive and reachable

Each contextfree Grammar G=(N,T,P,S) with  $\mathcal{L}(G)\neq\emptyset$  can be converted in  $\mathit{lineartime}$  into a reduced Grammar G' with

 $\mathcal{L}(G) = \mathcal{L}(G')$ 

Reduced Grammars - Construction:

Compute the subset  $N_1\subseteq N$  of all produktive nonterminals of G. Since  $\mathcal{L}(G)\neq\emptyset$  in particular  $S\in N_1$ .

2. Step:

 $P_1 = \{ A \to \alpha \in P \mid A \in N_1 \land \alpha \in (N_1 \cup T)^* \}$ 

3. Step: Compute the subset  $N_2\subseteq N_1$  of all productive and reachable nonterminals of G.

Since  $\mathcal{L}(G) \neq \emptyset$  in particular  $S \in N_2$ 

4. Step:

Construct:  $P_2 = \{A \rightarrow \alpha \in P \mid A \in N_2 \land \alpha \in (N_2 \cup T)^*\}$ 

Result:  $G' = (N_2, T, P_2, S)$ 

Reduced Grammars - Example:

Chapter 2:

Basics of Pushdown Automata

Basics of Pushdown Automata

Languages, specified by context free grammars are accepted by Pushdown Automata:

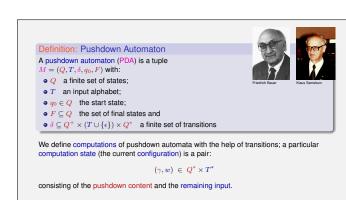


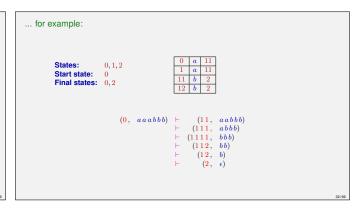
The pushdown is used e.g. to verify correct nesting of braces.

Example:

States: 0.1.2Start state: 0 Final states: 0,2

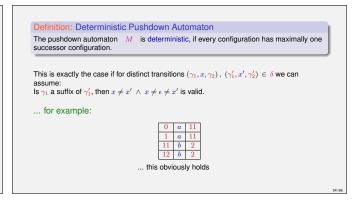
- We do not differentiate between pushdown symbols and states
- The rightmost / upper pushdown symbol represents the state
- Every transition consumes / modifies the upper part of the pushdown

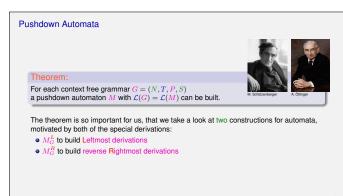


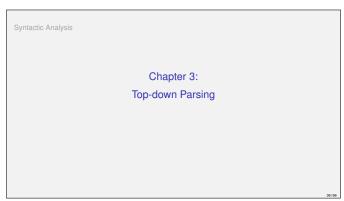


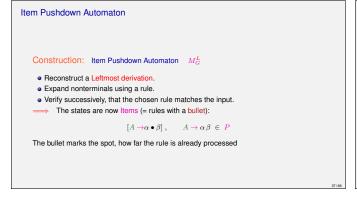
A computation step is characterized by the relation  $\vdash \subseteq (Q^* \times T^*)^2$  with  $(\alpha\gamma, xw) \vdash (\alpha\gamma', w)$  for  $(\gamma, x, \gamma') \in \delta$  Remarks:

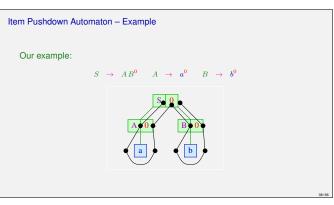
• The relation  $\vdash$  depends on the pushdown automaton M• The reflexive and transitive closure of  $\vdash$  is denoted by  $\vdash^*$ • Then, the language accepted by M is  $\mathcal{L}(M) = \{w \in T^* \mid \exists f \in F : (q_0, w) \vdash^* (f, \epsilon)\}$ We accept with a final state together with empty input.

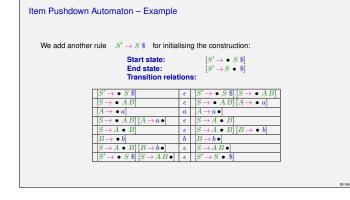


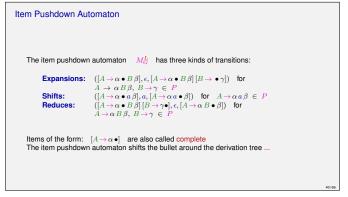












### Item Pushdown Automaton

### Discussion:

- The expansions of a computation form a leftmost derivation
- Unfortunately, the expansions are chosen nondeterministically
- $\bullet$  For proving correctness of the construction, we show that for every Item  $\ [A \to \alpha \bullet B \ \beta]$  the following holds:

$$([A \to \alpha \bullet B \beta], w) \vdash^* ([A \to \alpha B \bullet \beta], \epsilon)$$
 iff  $B \to^* w$ 

 LL-Parsing is based on the item pushdown automaton and tries to make the expansions deterministic ...

### 

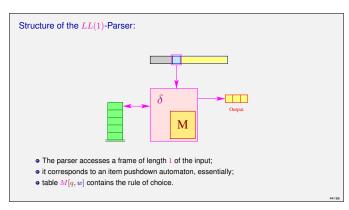
Conflicts arise between the transitions (0,1) and (3,4), resp..

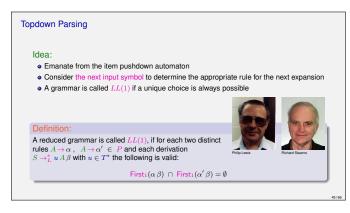
Problem:
Conflicts between the transitions prohibit an implementation of the item pushdown automaton as deterministic pushdown automaton.

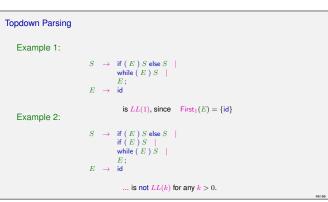
Idea 1: GLL Parsing
For each conflict, we create a virtual copy of the complete configuration and continue computing in parallel.

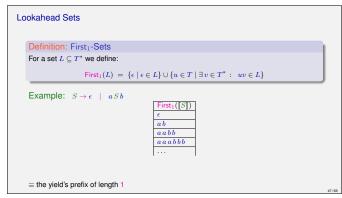
Idea 2: Recursive Descent & Backtracking
Depth-first search for an appropriate derivation.

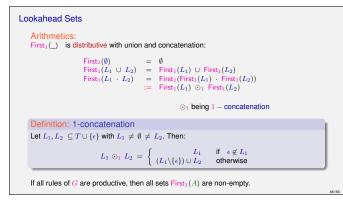
Idea 3: Recursive Descent & Lookahead
Conflicts are resolved by considering a lookup of the next input symbols.

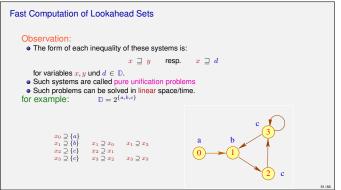


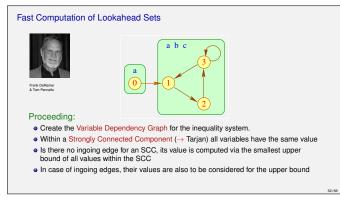


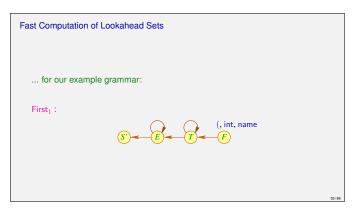


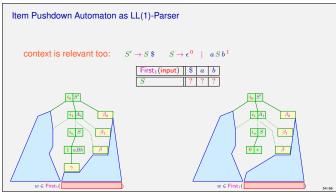


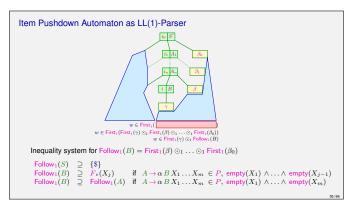


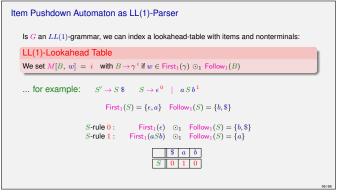


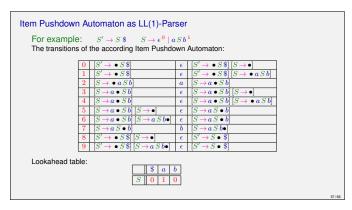


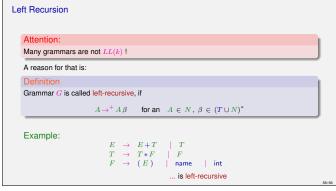


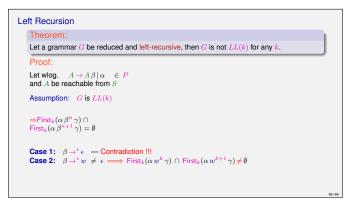












```
Right-Regular Context-Free Parsing
Recurring scheme in programming languages: Lists of sth... S \to b \mid Sab
Alternative idea: Regular Expressions S \to (ba)^*b
Definition: Right-Regular Context-Free Grammar
A right-regular context-free grammar (RR-CFG) is a 4-tuple G = (N, T, P, S) with:

• N the set of nonterminals,
• T the set of terminals,
• P the set of trules with regular expressions of symbols as rhs,
• S \in N the start symbol

Example: Arithmetic Expressions
S \to E
E \to T(+T)^*
T \to F(*F)^*
F \to (E) | name | int
```

```
\begin{array}{c} \textbf{Definition:} \\ \textbf{An } RR-CFG \ \textit{G} \ \text{is called } RLL(1), \\ \textbf{if the corresponding } CFG \ \langle G \rangle \ \text{is an } LL(1) \ \text{grammar.} \\ \hline \textbf{Discussion} \\ \bullet \ \text{directly yields the table driven parser } M_{(G)}^L \ \text{for } RLL(1) \ \text{grammars} \\ \bullet \ \text{however: mapping regular expressions to recursive productions unnessessarily strains } \\ \textbf{the stack} \\ \rightarrow \ \text{instead directly construct automaton in the style of Berry-Sethi} \\ \end{array}
```

```
Idea 2: Recursive Descent RLL Parsers:
    Recursive descent RLL(1)-parsers are an alternative to table-driven parsers; apart from
    the usual function scan(), we generate a program frame with the lookahead function
    expect() and the main parsing method parse():
        int next;
        void expect(Set E){
            if ({e, next} \cap E = \emptyset){
                  cerr << "Expected" << E << "found" << next;
            exit(0);
        }
        return;
        }
        void parse(){
            next = scan();
            expect(First_1(S));
        S();
            expect(EDF});
    }
}</pre>
```

```
Discussion

A practical implementation of an RLL(1)-parser via recursive descent is a straight-forward idea

However, only a subset of the deterministic contextfree languages can be parsed this way.

As soon as First₁(_) sets are not disjoint any more,

Solution 1: For many accessibly written grammars, the alternation between right hand sides happens too early. Keeping the common prefixes of right hand sides joined and introducing a new production for the actual diverging sentence forms often helps.

Solution 2: Introduce ran/ked grammars, and decide conflicting lookahead always in favour of the higher ranked alternative

→ relation to LL parsing not so clear any more

→ not so clear for _* operator how to decide

Solution 3: Coing from LL(1) to LL(k)

The size of the occurring sets is raighdly increasing with larger k

Unfortunately, even LL(k) parsers are not sufficient to accept all deterministic contextfree languages. (regular lookahead → LL(*))

In practical systems, this often motivates the implementation of k = 1 only ...
```

```
Topic:
Syntactic Analysis - Part II
```

```
Syntactic Analysis - Part II

Chapter 1:

Bottom-up Analysis
```

```
Shift-Reduce Parser

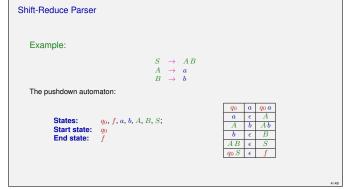
Idea:

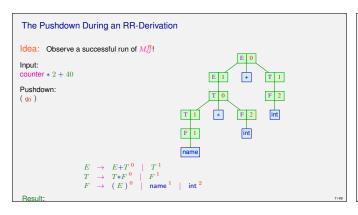
We delay the decision whether to reduce until we know, whether the input matches the right-hand-side of a rule!

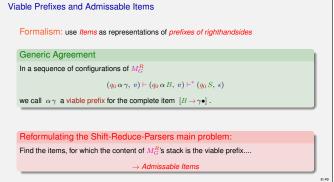
Construction: Shift-Reduce parser M_G^R

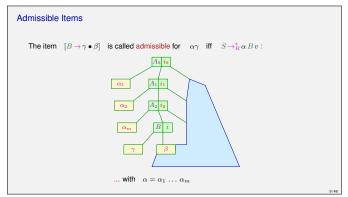
The input is shifted successively to the pushdown.

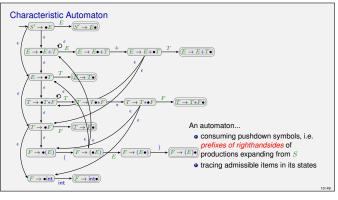
Is there a complete right-hand side (a handle) atop the pushdown, it is replaced (reduced) by the corresponding left-hand side
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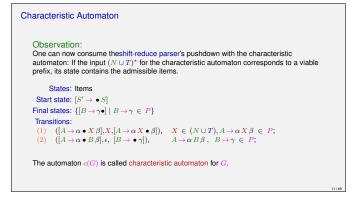


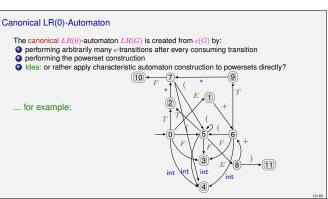


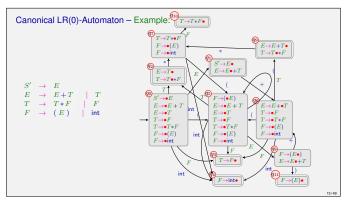


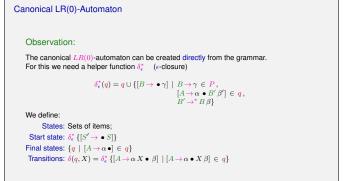


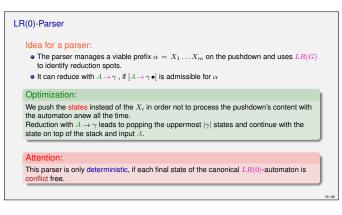


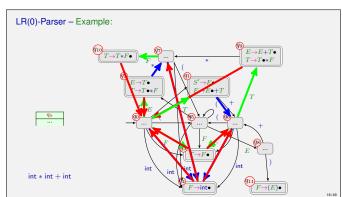


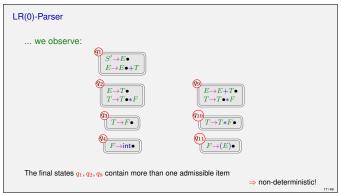


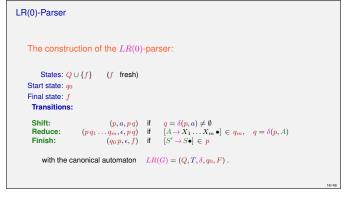


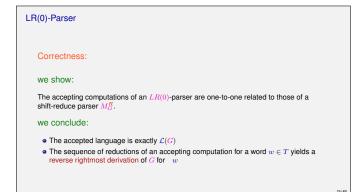


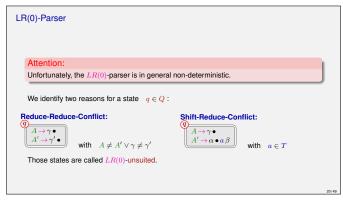


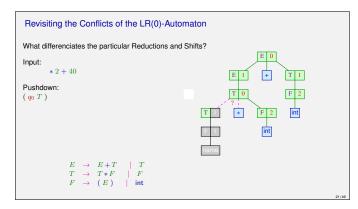


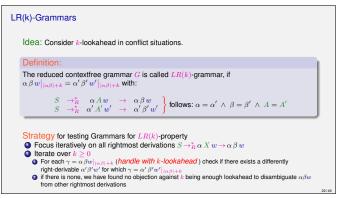


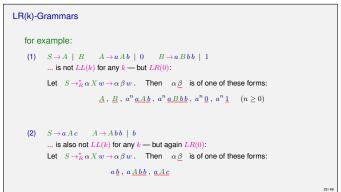






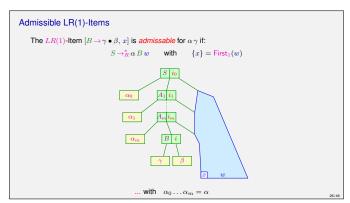






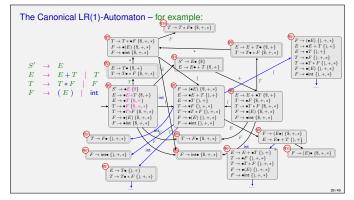
```
for example: 

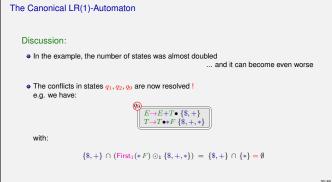
(3) S \rightarrow a\,A\,c A \rightarrow b\,b\,A \mid b ... is not LR(0), but LR(1): Let S \rightarrow_R^* \alpha X \, w \rightarrow \alpha \beta \, w with \{y\} = \mathsf{First}_k(w) then \alpha \, \underline{\beta} \, y is of one of these forms: a \, b^{2n} \, \underline{b} \, c \, , \, a \, b^{2n} \, \underline{b} \, \underline{b} \, A \, c \, , \, \underline{a} \, \underline{A} \, c (4) S \rightarrow a\,A\,c A \rightarrow b\,A\,b \mid b ... is not LR(k) for any k \geq 0: Consider the rightmost derivations: S \rightarrow_R^* a \, b^n \, A \, b^n \, c \rightarrow a \, b^n \, \underline{b} \, b^n \, c
```

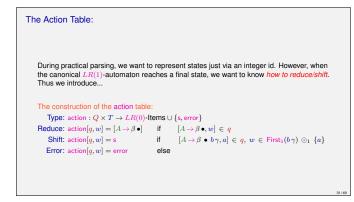


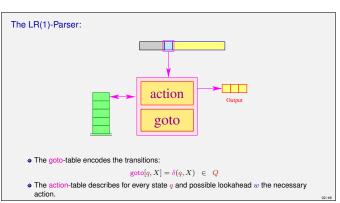
```
The Characteristic LR(1)-Automaton  \begin{array}{l} \text{The set of admissible $LR(1)$-items for viable prefixes is again computed with the help of the finite automaton $c(G,1)$.} \\ \text{The automaton $c(G,1)$:} \\ \text{States: $LR(1)$-items} \\ \text{Start state: $[S' \to \bullet S, \$]$} \\ \text{Final states: $\{[B \to \gamma \bullet, x] \mid B \to \gamma \in P, x \in \text{Follow}(B)\}$} \\ \text{(1) $([A \to \alpha \bullet X \beta, x], X, [A \to \alpha X \bullet \beta, x]), $X \in (N \cup T)$} \\ \text{Transitions: (2) $([A \to \alpha \bullet B \beta, x], \epsilon, [B \to \bullet \gamma, x']), $A \to \alpha B \beta, B \to \gamma \in P, $x' \in \text{First}_1(\beta) \odot_1 \{x\}$} \\ \text{This automaton works like $c(G)$ — but additionally manages a 1-prefix from Follow1 of the left-hand sides.} \\ \end{array}
```

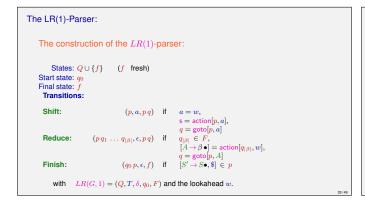
```
The Canonical LR(1)-Automaton  \begin{aligned} & \text{The canonical LR}(1)\text{-automaton }LR(G,1) \text{ is created from }c(G,1), \text{ by performing arbitrarily many $\epsilon$-transitions and then making the resulting automaton deterministic ...} \\ & \text{But again, it can be constructed directly from the grammar; analoguously to }LR(0), \text{ we need the $\epsilon$-closure $\delta_\epsilon^*$ as a helper function: } \\ & \delta_\epsilon^*(q) = q \cup \{[C \to \bullet \gamma, x] \mid [A \to \alpha \bullet B \beta', x'] \in q, \quad B \to^* C \beta, \quad C \to \gamma \in P, \\ & x \in \mathsf{First}_1(\beta \beta') \odot_1 \{x'\}\} \end{aligned}  Then, we define:  \begin{aligned} & \text{States: Sets of } LR(1)\text{-items;} \\ & \text{States: Sets of } LR(1)\text{-items;} \\ & \text{Start state: $\delta_\epsilon^* \{[S' \to \bullet S, \$]\} } \\ & \text{Final states: $\{q \mid |A \to \alpha \bullet x] \in q\} } \\ & \text{Transitions: $\delta(q, X) = \delta_\epsilon^* \{[A \to \alpha X \bullet \beta, x] \mid [A \to \alpha \bullet X \beta, x] \in q\} \end{aligned}
```

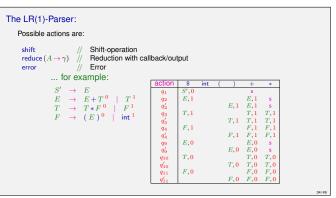


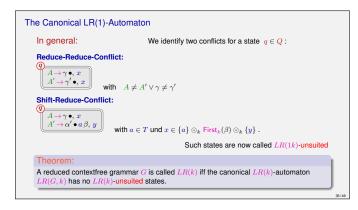


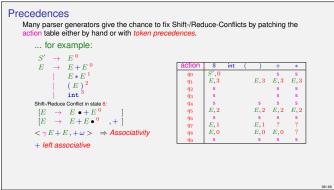


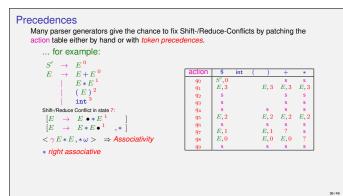


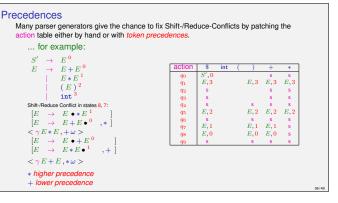


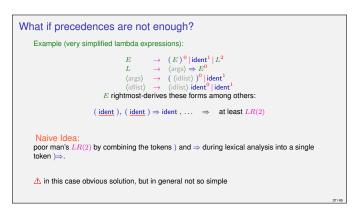


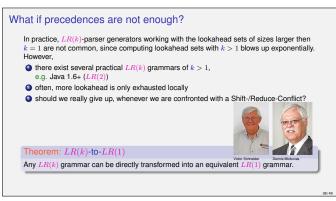


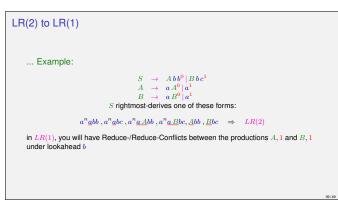


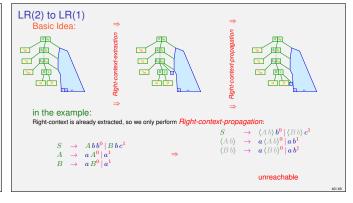


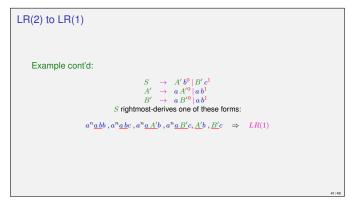


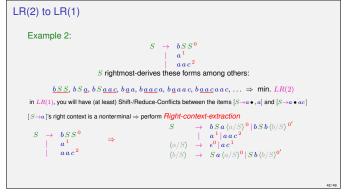












```
LR(2) to LR(1)

Example 2 cont'd: [S \rightarrow a] \text{'s right context is now terminal } a \Rightarrow \text{perform } \underset{\text{$Right-context-propagation}}{Right-context-propagation}
S \rightarrow b \langle Sa \rangle \langle a/S \rangle^0 \\ | bSb \langle b/S \rangle^0 \\ | a^1 | aac^2 \\ | bSb \langle b/S \rangle^0 \\ | a^1 | aac^2 \\ | a^1 | aac^2 \\ | a^1 | aac^2 \\ | a^1 | aac^1 \\ | (b/S) \rightarrow e^0 | ac^1 \\ | (b/S) \rightarrow Sa \langle a/S \rangle^0 | Sb \langle b/S \rangle^0 \\ | a^1 | aac^2 \\ | (a/S) \rightarrow e^0 | ac^1 \\ | (b/S) \rightarrow Sa \langle a/S \rangle^0 | Sb \langle b/S \rangle^0 \\ | a^1 | aac^2 \\ | (a/S)a \rightarrow a^0 | acc^1 \\ | (a/S)a \rightarrow a^
```

```
Example 2 finished:
With fresh nonterminals we get the final grammar S \rightarrow bCA_{,0}^{0} | bSbB_{,1}^{1} | a^{2} | aac^{3}
S \rightarrow bSS^{0} \qquad \qquad A \rightarrow \epsilon^{0} | ac^{1}
| a^{1} \qquad \qquad C \rightarrow bCD^{0} | bSbE^{1} | aa^{2} | aaca^{3}
| aac^{2} \qquad D \rightarrow a^{0} | aca^{1}
E \rightarrow CD^{0} | SbE^{1}
```

```
Syntactic Analysis - Part II

Chapter 2:

LR(k)-Parser Design
```

```
LR(k)-Parser Design
       S' ::= E : e
                                          \{: RESULT = e;
                                                                                         Parser Actions
                     \begin{array}{ll} E \colon\! e \ \mathsf{plus} \ T \colon\! t & \{ \colon \ \mathsf{RESULT} = \mathsf{e} + \mathsf{t}; \quad \colon\! \} \\ T \colon\! t & \{ \colon \ \mathsf{RESULT} = \mathsf{t}; \quad \colon\! \} \\ \end{array} 
                                                                                           For each rule, specify user code to
                                                                                           be executed in case of reduction
                                                                                           actions.
                    \begin{array}{ll} T : t \ \mathsf{times} \ F : f & \{ : \ \ \mathsf{RESULT} = \mathtt{t} \ast \mathtt{f}; & : \} \\ F : f & \{ : \ \ \mathsf{RESULT} = \mathtt{f}; & : \} \end{array}

    add code sections delimited with

                                                                                                 {: :} to each variant
                    produce results by assigning
                                                                                                values to RESULT
                                                                                            add labels to symbols to refer to
                                                                                                 former results
     Implementation Idea: add data stack that
        • pushes RESULT after each user action

    translates labeled symbols to offset from top of stack based on the position in the rhs
```

```
A Practial Example: Type Definitions in ANSI C

A type definition is a synonym for a type expression.
In C they are introduced using the typedef keyword.
Type definitions are useful

• as abbreviation:

typedef struct { int x; int y; } point_t;

• to construct recursive types:

Possible declaration in C: more readable:

typedef struct list list_t;

struct list { int info;

struct list { int info;

struct list* next; } list_t* next;

} struct list* head; list_t* head;
```

```
Topic:
Semantic Analysis
```

```
Scanner and parser accept programs with correct syntax.

• not all programs that are syntactically correct make sense

• the compiler may be able to recognize some of these

• these programs are rejected and reported as erroneous

• the language definition defines what erroneous means

• semantic analyses are necessary that, for instance:

• check that identifiers are known and where they are defined

• check the type-correct use of variables

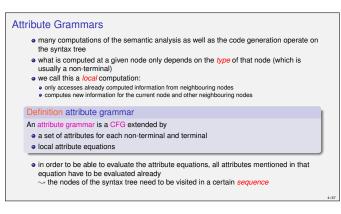
• semantic analyses are also useful to

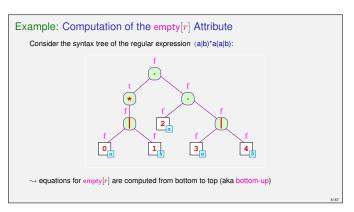
• find possibilities to "optimize" the program

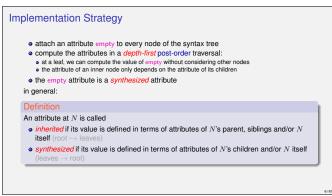
• warn about possibly incorrect programs

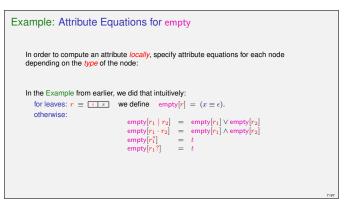
a semantic analysis annotates the syntax tree with attributes
```

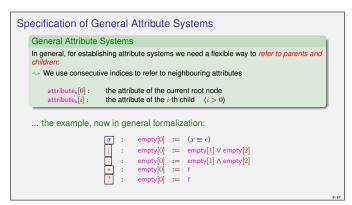
```
Chapter 1:
Attribute Grammars
```











```
Observations

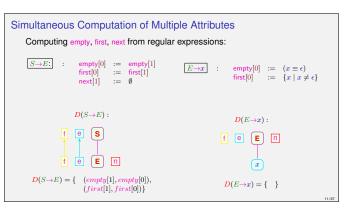
• the local attribute equations need to be evaluated using a global algorithm that knows about the dependencies of the equations
• in order to construct this algorithm, we need
• a sequence in which the nodes of the tree are visited
• a sequence within each node in which the equations are evaluated
• this evaluation strategy has to be compatible with the dependencies between attributes

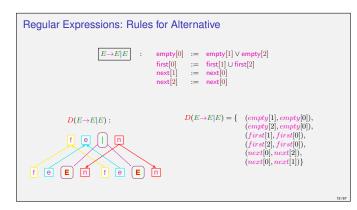
We visualize the attribute dependencies D(p) of a production p in a Local Dependency Graph:

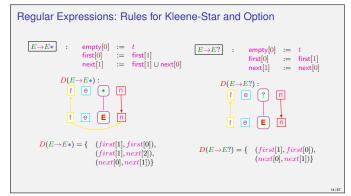
Let p = N<sub>0</sub> → N<sub>1</sub>|N<sub>2</sub> in

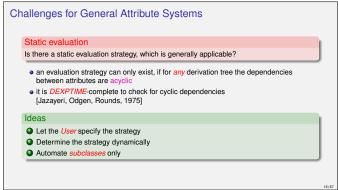
D(p) = { (empty[1], empty[0]), (empty[2], empty[0])}

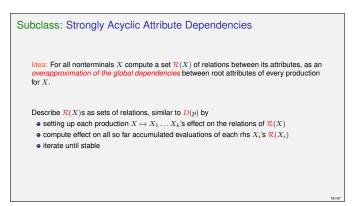
→ arrows point in the direction of information flow
```

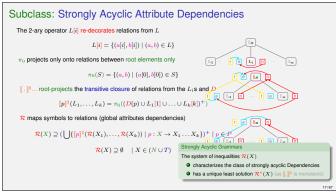


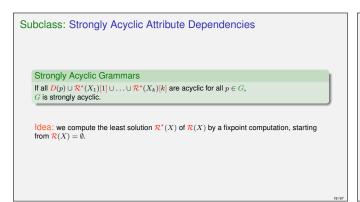


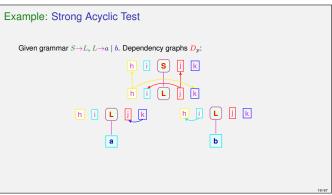


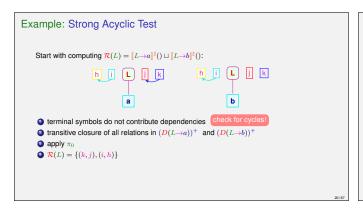


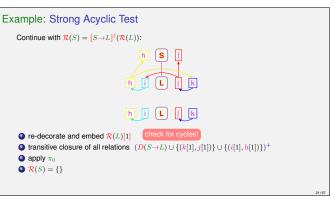


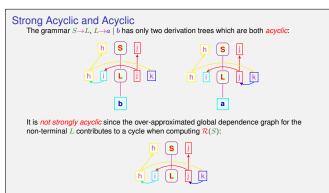


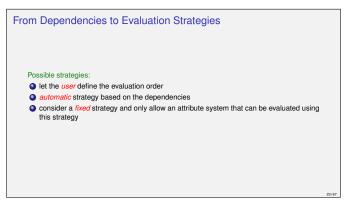


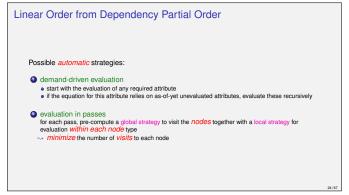


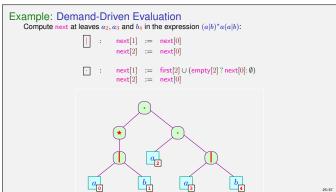




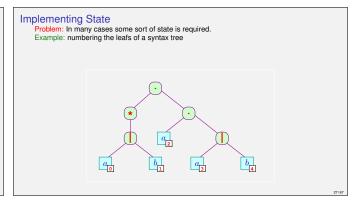


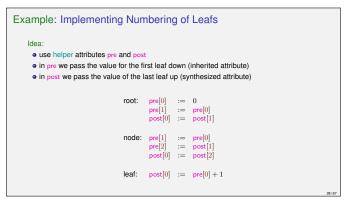


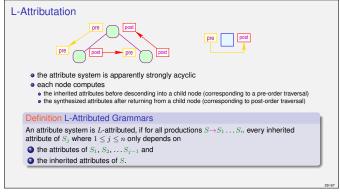




## Demand-Driven Evaluation Observations • each node must contain a pointer to its parent • only required attributes are evaluated • the evaluation sequence depends – in general – on the actual syntax tree • the algorithm must track which attributes it has already evaluated • the algorithm may visit nodes more often than necessary → the algorithm is not local in principle: • evaluation strategy is dynamic: difficult to debug • usually all attributes in all nodes are required → computation of all attributes is often cheaper → perform evaluation in passes







### L-Attributation

### Background:

- $\bullet$  the attributes of an  $L\text{-}\mathrm{attributed}$  grammar can be evaluated during parsing
- important if no syntax tree is required or if error messages should be emitted while parsing
- example: pocket calculator

L-attributed grammars have a fixed evaluation strategy:

a single *depth-first* traversal

- ullet in general: partition all attributes into  $\mathcal{A}=A_1\cup\ldots\cup A_n$  such that for all attributes in  $A_i$  the attribute system is L-attributed
- ullet perform a depth-first traversal for each attribute set  $A_i$
- $\sim$  craft attribute system in a way that they can be partitioned into few L-attributed sets

### **Practical Applications**

- $\bullet$  symbol tables, type checking/inference, and simple code generation can all be specified using L-attributed grammars
- most applications *annotate* syntax trees with additional information
- the nodes in a syntax tree usually have different types that depend on the non-terminal that the node represents
- the different types of non-terminals are characterized by the set of attributes with which they are decorated

### Example: Def-Use Analysis

- a statement may have two attributes containing valid identifiers: one ingoing (inherited) set and one outgoing (synthesised) set
- an expression only has an ingoing set

```
Example: Leaf Numbering

public abstract class AbstractVisitor implements Visitor {

public void pre (OrEx re) { pr(re); }

public void pre (AndEx re) { pr(re); }

public void pre (AndEx re) { pr(re); }

public void post (OrEx re) { po(re); }

public void post (OrEx re) { po(re); }

public void post (AndEx re) { po(re); }

abstract void po (BinEx re);

abstract void in (BinEx re);

abstract void pr(BinEx re);

}

public class LeafNum extends AbstractVisitor {

public Map<Regex, Integer> pre = new HashMap<>();

public LeafNum (Regex re) { pre .put(r,0); r.accept(this); }

public LeafNum (Regex re) { pre .put(r,0); r.accept(this); }

public void pre (Const r) { post.put(r, pre .get(r)+1); }

public void in (BinEx r) { pre .put(r.r, post.get(r.1)); }

public void po (BinEx r) { pre .put(r.r, post.get(r.r)); }

public void po (BinEx r) { post.put(r, post.get(r.r)); }

public void po (BinEx r) { post.put(r, post.get(r.r)); }
```

```
Chapter 2:
Decl-Use Analysis
```

```
Symbol Bindings and Visibility

Consider the following Java code:

void foo() {
  int a;
  while (true) {
    double a;
    a = 0.5;
    write(a);
    break;
  }
  a = 2;
  bar();
  write(a);
  }
  vrite(a);
  bar();
  write(a);
  }
}

a = 2;
  bar();
  write(a);
  bar();
  write(a);
  break;
}

a = bar();
  write(a);
  cach declaration of a variable v causes memory allocation for v

  e using v requires knowledge about its memory location
  cation → determine the declaration v is bound to
  in the same name is in scope
  in the example the declaration of a is shadowed by the local declaration in the loop body
```

```
Scope of Identifiers

void foo() {
    int a;
    while (true) {
        double a;
        a = 0.5;
        write(a);
        break;
    }
    a = 2;
    bar();
    write(a);
    double a

A administration of identifiers can be quite complicated...
```

```
Resolving Identifiers

Observation: each identifier in the AST must be translated into a memory access

Problem: for each identifier, find out what memory needs to be accessed by providing rapid access to its declaration

Ideas:

■ rapid access: replace every identifier by a unique integer

→ integers as keys: comparisons of integers is faster

■ link each usage of a variable to the declaration of that variable

→ for languages without explicit declarations, create declarations when a variable is first encountered
```

```
Rapid Access: Replace Strings with Integers

Idea for Algorithm:
Input: a sequence of strings
Output: ① sequence of numbers
① table that allows to retrieve the string that corresponds to a number Apply this algorithm on each identifier during scanning.

Implementation approach:
② count the number of new-found identifiers in int count
③ maintain a hashtable S: String \to int to remember numbers for known identifiers

We thus define the function:

int indexForldentifier(String w) {
    if (S(w) \equiv undefined) {
        S = S \oplus \{w \mapsto count\};
        return count++;
} else return S(w);
```

```
Implementation: Hashtables for Strings

allocate an array M of sufficient size m
choose a hash function H: \mathbf{String} \to [0, m-1] with:

be H(w) is cheap to compute
definition H: \mathbf{String} \to [0, m-1] with:

be H(w) is cheap to compute
definition H: \mathbf{String} \to [0, m-1]

Possible generic choices for sequence types (\vec{x} = \langle x_0, \dots x_{r-1} \rangle):

H_0(\vec{x}) = (x_0 + x_{r-1}) \% m
H_1(\vec{x}) = (\sum_{i=0}^{r-1} a_i \cdot p^i) \% m
= (x_0 + p \cdot (x_1 + p \cdot (\dots + p \cdot x_{r-1} \cdots))) \% m
for some prime number p (e.g. 31)

X The hash value of w may not be uniquel
\to \text{Append } (w, i) \text{ to a linked list located at } M[H(w)]
\to \text{Finding the index for } w, we compare w with all x for which H(w) = H(x)

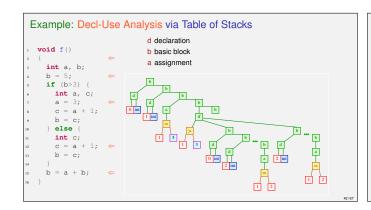
x access on average:
insert: \mathcal{O}(1)
lookup: \mathcal{O}(1)
```

```
Example: Replacing Strings with Integers
   Input:
| Peter | Piper | picked | a | peck | of | pickled | peppers
   If Peter Piper picked a peck of pickled peppers
    wheres the peck of pickled peppers Peter Piper picked
   Hashtable with m = 7 and H_0:
     0 Peter
                     6 pickled
7 peppers
                                            0 If 8 the 10
         Piper
     2 picked
3 a
4 peck
                                                pickled 6 peck 4 picked 2
of 5 wheres 9 peppers 7
                      8
                          wheres
                      10 the
                                                Piper 1 Peter 0 a 3
     5 of
```

```
Check for the correct usage of variables:

• Traverse the syntax tree in a suitable sequence, such that
• each declaration is visited before its use
• the currently visible declaration is the last one visited

· perfect for an L-attributed grammar
• equation system for basic block must add and remove identifiers
• for each identifier, we manage a stack of declarations
• if we visit a declaration, we push it onto the stack of its identifier
• upon leaving the scope, we remove it from the stack
• if we visit a usage of an identifier, we pick the top-most declaration from its stack
• if the stack of the identifier is empty, we have found an undeclared identifier
```



```
Alternative Implementations for Symbol Tables

• when using a list to store the symbol table, storing a marker indicating the old head of the list is sufficient

• in front of if-statement then-branch else-branch

• instead of lists of symbols, it is possible to use a list of hash tables 

more elficient in large, shallow programs

• an even more elegant solution: persistent trees (updates return fresh trees with references to the old tree where possible)

a persistent tree t can be passed down into a basic block where new elements may be added, yielding a t'; after examining the basic block, the analysis proceeds with the unchanged old t
```

```
Semantic Analysis

Chapter 3:
Type Checking
```

```
In most mainstream (imperative / object oriented / functional) programming languages, variables and functions have a fixed type.

for example: int, void*, struct { int x; int y; }.

Types are useful to

manage memory

select correct assembler instructions

to avoid certain run-time errors

In imperative and object-oriented programming languages a declaration has to specify a type. The compiler then checks for a type correct use of the declared entity.
```

```
Type Expressions

Types are given using type-expressions. The set of type expressions T contains:

• base types: int, char, £loat, void, ...

• type constructors that can be applied to other types example for type constructors in C:

• structures: struct { t_1 a_1; ... t_k a_k; }

• pointers: t *

• arrays: t []

• the size of an array can be specified
• the variable to be declared is written between t and [n]
• functions: t (t_1, \ldots, t_k)
• the variable to be declared is written between t and t_1, \ldots, t_k)
• in ML function types are written as: t_1 * \ldots * t_k \to t
```

```
Problem:
Given: A set of type declarations Γ = {t<sub>1</sub> x<sub>1</sub>;...t<sub>m</sub> x<sub>m</sub>;}
Check: Can an expression e be given the type t?

Example:

struct list { int info; struct list* next; };
int f(struct list* 1) { return 1; };
struct { struct list* c;}* b;
int* a[11];

Consider the expression:

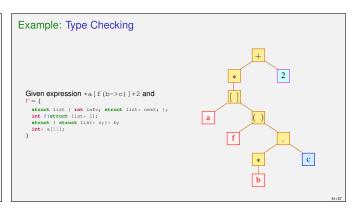
*a[f(b->c)]+2;
```

```
Type Checking using the Syntax Tree

Check the expression *a [f (b->c)]+2:

| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
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| Check the expression *a [f (b->c)]+2:
| Check the expression *a [f (b->c)]+2:
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| Check th
```

```
Type Systems for C-like Languages
       More rules for typing an expression: with subtyping relation \( \leq \)
                                                                 Array:
                Array:
                                                              \Gamma \vdash e : \mathbf{struct} \{t_1 \ a_1; \dots t_m \ a_m; \}
                Struct:
                                       \frac{\Gamma \vdash e : t(t_1, \dots, t_m) \quad \Gamma \vdash e_1 : t_1}{\Gamma \vdash e(e_1, \dots, e_m) : t}
                                                                                   \Gamma \vdash e_1 : t_1 \ldots \Gamma \vdash e_m : t_m
                App:
                                                                   \frac{\Gamma \vdash e_1 : t_1 \quad \Gamma \vdash e_2 : t_2}{\Gamma \vdash e_1 \square e_2 : t_1 \square t_2}
                On □:
                                          \frac{\Gamma \vdash e_1 \ : \ t_1 \qquad \Gamma \vdash e_2 \ : \ t_2 \quad t_2 \text{ can be converted to} \leq t_1}{\Gamma \vdash e_1 = e_2 \ : \ t_1}
                Op =:
                                                        \frac{\Gamma \vdash e \ : \ t_2 \qquad t_2 \text{ can be converted to} \leq t_1}{\Gamma \vdash (t_1) \ e \ : \ t_1}
                Explicit Cast:
```



```
Example: Type Checking — More formally: \Gamma = \left\{\begin{array}{l} \text{struct list { int info; struct list* next; };} \\ \text{struct list { int info; struct list* next; };} \\ \text{struct { struct list* c;} * b;} \\ \text{struct { struct list* c;} * b;} \\ \text{STRUCT} & \hline \frac{\mathsf{DEREF}}{\Gamma \vdash b : \mathsf{struct[struct list* 'C;]*}} \\ \hline \Gamma \vdash *b : \mathsf{struct[struct list* 'C;]*} \\ \hline \Gamma \vdash *b : \mathsf{struct[struct list* 'C;]*} \\ \hline \Gamma \vdash *b : \mathsf{struct[struct list* 'C;]*} \\ \hline \Gamma \vdash *b : \mathsf{struct[struct list* 'C;]*} \\ \hline \Gamma \vdash *b : \mathsf{struct[struct list* 'C]*} \\ \hline \Gamma \vdash *f(b \to c) : \mathsf{int} \checkmark \\ \hline \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \checkmark \\ \hline \mathsf{OP} & \hline \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \end{cases} \\ \hline \mathsf{DEREF}} & \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \end{cases} & \mathsf{Const} \\ \hline \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \checkmark \\ \mathsf{Deres} & \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \end{cases} \\ \mathsf{Deres} & \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \end{cases} & \mathsf{Donst} \\ \mathsf{Deres} & \Gamma \vdash *a[f(b \to c)] : \mathsf{int} \end{cases} & \mathsf{Donst} \\ \mathsf{Deres} & \mathsf{Deres} &
```

```
Equality of Types =

Summary of Type Checking

• Choosing which rule to apply at an AST node is determined by the type of the child nodes

• determining the rule requires a check for ~ equality of types

type equality in C:

• struct A {} and struct B {} are considered to be different

• ~ the compiler could re-order the fields of A and B independently (not allowed in C)

• to extend an record A with more fields, it has to be embedded into another record:

struct B {
 struct A;
 int field_of_B;
 } extension_of_A;

• after issuing typedef int C; the types C and int are the same
```

```
Structural Type Equality

Alternative interpretation of type equality (does not hold in C):

semantically, two types t<sub>1</sub>, t<sub>2</sub> can be considered as equal if they accept the same set of access paths.

Example:
struct list {
int info;
struct list* next;
} struct {
int info;
struct list* next;
} * next;

Consider declarations struct list* 1 and struct list1* 1. Both allow
1->info 1->next->info

but the two declarations of 1 have unequal types in C.
```

```
Algorithm for Testing Structural Equality

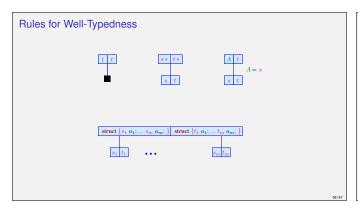
Idea:

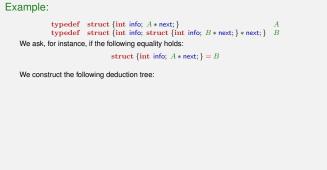
• track a set of equivalence queries of type expressions
• if two types are syntactically equal, we stop and report success
• otherwise, reduce the equivalence query to a several equivalence queries on (hopefully) simpler type expressions

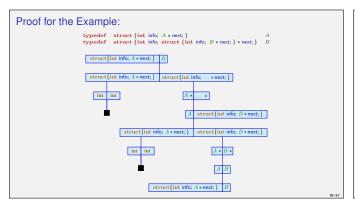
Suppose that recursive types were introduced using type definitions:

typedef A t

(we omit the □). Then define the following rules:
```





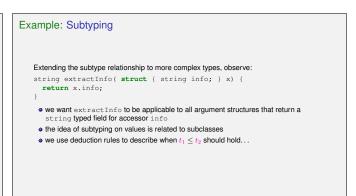


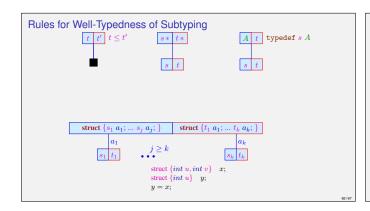
## Implementation We implement a function that implements the equivalence query for two types by applying the deduction rules: • if no deduction rule applies, then the two types are not equal • if the deduction rule for expanding a type definition applies, the function is called recursively with a potentially larger type • in case an equivalence query appears a second time, the types are equal by definition Termination • the set D of all declared types is finite • there are no more than |D|² different equivalence queries • repeated queries for the same inputs are automatically satisfied termination is ensured

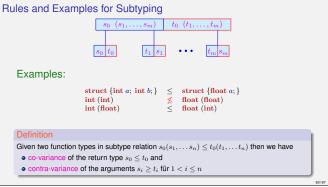
```
Subtyping \leq

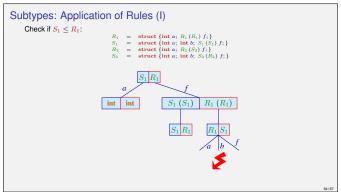
On the arithmetic basic types char, int, long, etc. there exists a rich subtype hierarchy Subtypes t_1 \leq t_2, means that the values of type t_1 of orm a subset of the values of type t_2; of can be converted into a value of type t_2; of fulfill the requirements of type t_2; are assignable to variables of type t_2.

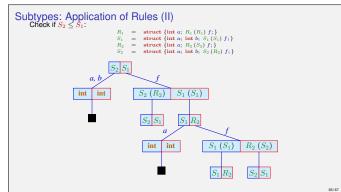
Example: assign smaller type (fewer values) to larger type (more values) t_1 int x; t_2 double y; y=x; t_1 \leq t_2 int \leq double
```

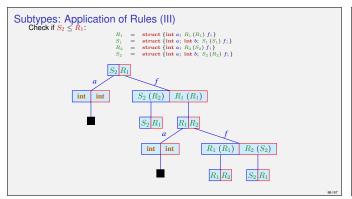












## • for presentational purposes, proof trees are often abbreviated by omitting deductions within the tree • structural sub-types are very powerful and can be quite intricate to understand • Java generalizes structs to objects/classes where a sub-class A inheriting form base class O is a subtype A ≤ O • subtype relations between classes must be explicitly declared

# Topic: Code Synthesis

Generating Code: Overview

We inductively generate instructions from the AST:

• there is a rule stating how to generate code for each non-terminal of the grammar

• the code is merely another attribute in the syntax tree

• code generation makes use of the already computed attributes

In order to specify the code generation, we require

• a semantics of the language we are compiling (here: C standard)

• a semantics of the machine instructions

~ we commence by specifying machine instruction semantics

Chapter 1:
The Register C-Machine

The Register C-Machine (R-CMa)

We generate Code for the Register C-Machine.
The Register C-Machine is a virtual machine (VM).

• there exists no processor that can execute its instructions
• ... but we can build an interpreter for it
• we provide a visualization environment for the R-CMa
• the R-CMa has no double, float, char, short or long types
• the R-CMa has no instructions to communicate with the operating system
• the R-CMa has an unlimited supply of registers

The R-CMa is more realistic than it may seem:
• the mentioned restrictions can easily be lifted
• the Dalvik VM/ART or the LLVM are similar to the R-CMa
• an interpreter of R-CMa can run on any platform

# Virtual Machines A virtual machine has the following ingredients: any virtual machine provides a set of instructions instructions are executed on virtual hardware the virtual hardware is a collection of data structures that is accessed and modified by the VM instructions ... and also by other components of the run-time system, namely functions that go beyond the instruction semantics the interpreter is part of the run-time system

Components of a Virtual Machine
Consider Java as an example:

C

0 1

PC

S

A virtual machine such as the Dalvik VM has the following structure:

• S: the data store – a memory region in which cells can be stored in LIFO order ~ stack.

• SP: (= stack pointer) pointer to the last used cell in S

• beyond S follows the memory containing the heap

• C is the memory storing code

• each cell of C holds exactly one virtual instruction

• C can only be read

• PC (= program counter) address of the instruction that is to be executed next

• PC contains 0 initially

### **Executing a Program**

- the machine loads an instruction from C[PC] into the instruction register IR in order to
- before evaluating the instruction, the PC is incremented by one

```
while (true) {
  IR = C[PC]; PC++;
  execute (IR);
```

- node: the PC must be incremented before the execution, since an instruction may modify the PC
- the loop is exited by evaluating a halt instruction that returns directly to the operating

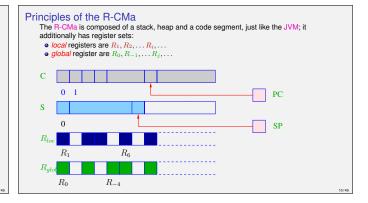
Code Synthesis Chapter 2: Generating Code for the Register C-Machine

### Simple Expressions and Assignments in R-CMa

Task: evaluate the expression (1+7)\*3

- that is, generate an instruction sequence that
- o computes the value of the expression and
- keeps its value accessible in a reproducable way

- first compute the value of the sub-expressions
- store the intermediate result in a temporary register
- apply the operator
- loop



### The Register Sets of the R-CMa

The two register sets have the following purpose:

- $\bigcirc$  the *local* registers  $R_i$ 

  - save temporary results
     store the contents of local variables of a function
     can efficiently be stored and restored from the stack
- the global registers R:
  - save the parameters of a function
    store the result of a function

for now, we only use registers to store temporary computations

Idea for the translation: use a register counter  $\it i$ :

- ullet registers  $R_j$  with j < i are in use
- ullet registers  $R_j$  with  $j \geq i$  are available

### Translation of Simple Expressions

Using variables stored in registers; loading constants:

instruction semantics intuition  $\begin{array}{lll} \text{loadc } R_i \ c & R_i = c & \text{load constant} \\ \text{move } R_i \ R_j & R_i = R_j & \text{copy } R_j \ \text{to } R_i \end{array}$ 

We define the following translation schema (with  $\rho \ x=a$ ):

 $code_{R}^{i} c \rho = loadc R_{i} c$  $\operatorname{code}_{\mathbf{R}}^{i} x \rho = \operatorname{move} R_{i} R_{a}$  $\operatorname{code}_{\mathbf{R}}^{i} x = e \ \rho = \operatorname{code}_{\mathbf{R}}^{i} e \ \rho$ move  $R_a$   $R_i$ 

### Translation of Expressions

 $\textit{Let op} = \{\textit{add}, \; \textit{sub}, \; \textit{div}, \; \textit{mul}, \; \textit{mod}, \; \textit{le}, \; \textit{gr}, \; \textit{eq}, \; \textit{leq}, \; \textit{geq}, \; \textit{and}, \; \textit{or}\}. \; \textit{The} \; \textit{R-CMa} \; \textit{provides} \;$ an instruction for each operator op.

where  $R_i$  is the target register,  $R_j$  the first and  $R_k$  the second argument.

Correspondingly, we generate code as follows:

 $\operatorname{code}_{R}^{i} e_{1} \operatorname{op} e_{2} \rho = \operatorname{code}_{R}^{i} e_{1} \rho$ op  $R_i$   $R_i$   $R_{i+1}$ 

Example: Translate 3\*4 with i=4:

 $code_{R}^{4} 3 * 4 \rho = loadc R_{4} 3$ 

mul R<sub>4</sub> R<sub>4</sub> R<sub>5</sub>

### Managing Temporary Registers

Observe that temporary registers are re-used: translate 3 \* 4 + 3 \* 4 with t = 4:

add  $R_4$   $R_4$   $R_5$ 

where

 $code_{R}^{i} 3 * 4 \rho = loadc R_{i} 3$ loadc  $R_{i+1}$  4 mul  $R_i$   $R_i$   $R_{i+1}$ 

we obtain

 $\operatorname{code}_{P}^{4} 3 \star 4 + 3 \star 4 \rho = \operatorname{loadc} R_{4} 3$ loade R<sub>5</sub> 4 mul R<sub>4</sub> R<sub>4</sub> R<sub>5</sub> loade Rx 3 loadc R<sub>6</sub> 4  $mul R_5 R_5 R_6$ add  $R_4$   $R_4$   $R_5$ 

### Semantics of Operators

The operators have the following semantics:

 $R_i = R_j + R_k$  $R_i = R_j - R_k$ add  $R_i R_j R_k$  $\begin{array}{c} \text{sub } R_i \ R_j \ R_k \\ \text{div } R_i \ R_j \ R_k \\ \text{mul } R_i \ R_j \ R_k \end{array}$  $R_i = R_j / R_k$   $R_i = R_j * R_k$  $\mod R_i \stackrel{\sim}{R_j} \stackrel{\sim}{R_k}$ le  $R_i R_j R_k$  $\begin{array}{l} \operatorname{gr} R_i \ R_j \ R_k \\ \operatorname{eq} R_i \ R_j \ R_k \\ \operatorname{leq} R_i \ R_j \ R_k \end{array}$ or  $R_i R_j R_k$ 

Note: all registers and memory cells contain operands in  $\ensuremath{\mathbb{Z}}$ 

### Translation of Unary Operators

Unary operators op =  $\{neg, not\}$  take only two registers:

 $\operatorname{code}^i_{\mathrm{R}}$  op  $e \ \rho = \operatorname{code}^i_{\mathrm{R}} \ e \ \rho$ op  $R_i$   $R_i$ 

Note: We use the same register.

Example: Translate -4 into  $R_5$ :

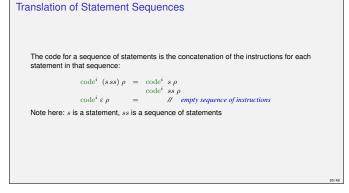
 ${\rm neg}\;R_5\;R_5$ 

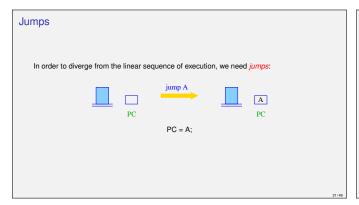
The operators have the following semantics:

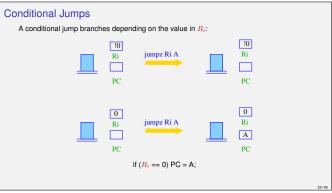
 $\begin{array}{ll} \operatorname{not}\,R_i\;R_j & \quad R_i \leftarrow \operatorname{if}\,R_j = 0 \text{ then } 1 \text{ else } 0 \\ \operatorname{neg}\,R_i\;R_j & \quad R_i \leftarrow -R_j \end{array}$ 

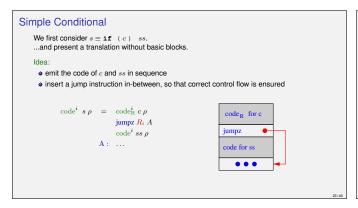
```
Applying Translation Schema for Expressions Suppose the following function void f (void) { is given: int x, y, z; x = y+z+3;  • Let \rho = \{x \mapsto 1, y \mapsto 2, z \mapsto 3\} be the address environment. • Let R_4 be the first free register, that is, i = 4. code^4 x = y+z+3 \rho = code^4_R y+z+3 \rho \mod R R_2 code^4_R y+z+3 \rho = move R_4 R_2 code^6_R z+3 \rho = move R_4 R_3 code^6_R z+3 \rho = move R_6 code^6_R z+3 \rho =
```

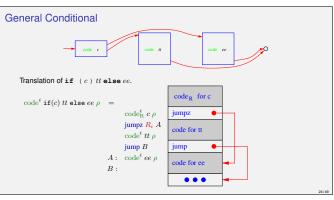
```
Chapter 3:
Statements and Control Structures
```

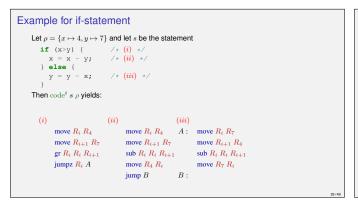


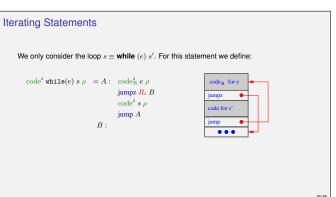












```
Example: Translation of Loops
     Let \rho = \{a \mapsto 7, b \mapsto 8, c \mapsto 9\} and let s be the statement:
        while (a>0) { /* (i) */
c = c + 1; /* (ii) */
a = a - b; /* (iii) */
     Then \operatorname{code}^i s \ \rho evaluates to:
                                 (ii)
                                     move R_i R_9
        (i)
                                                             (iii)

\begin{array}{ccc}
\text{move } R_i R_9 & \text{move } R_i R_7 \\
\text{loads } R_{i+1} 1 & & \\
\end{array}

        A: \text{ move } R_i R_7
                                                                        move R_{i+1} R_8
              loadc R_{i+1} 0
                                          add R_i R_i R_{i+1} sub R_i R_i R_{i+1}
               \operatorname{gr} R_i R_i R_{i+1}
                                       move R_9 R_i
               iumpz R_i B
                                                                       move R_7 R_i
                                                                        \mathsf{jump}\ A
```

```
Translation of the check^i Macro

The macro check^i l u B checks if l \le R_i < u. Let k = u - l.

• if l \le R_i < u it jumps to B + R_i - l

• if R_i < l or R_i \ge u it jumps to A_k we define:

check^i \ l \ u \ B = \begin{array}{c} \operatorname{loadc} R_{i+1} \ l \\ \operatorname{geq} R_{i+2} \ R_i \ R_{i+1} \\ \operatorname{jumpz} R_{i+2} \ E \end{array} \quad B: \quad \operatorname{jump} A_0
\operatorname{sub} R_i \ R_i \ R_{i+1} \quad \vdots \quad \vdots \\ \operatorname{loadc} R_{i+1} \ k \\ \operatorname{geq} R_{i+2} \ R_i \ R_{i+1} \\ \operatorname{jumpz} R_{i+2} \ D \qquad C:
E: \quad \operatorname{loadc} R_i \ k \\ D: \quad \operatorname{jumpi} R_i \ B
Note: a jump jumpi R_i \ B with R_i = u winds up at B + u, the default case
```

```
This translation is only suitable for certain switch-statement.

In case the table starts with 0 instead of u we don't need to subtract it from e before we use it as index

if the value of e is guaranteed to be in the interval [l,u], we can omit check
```

### General translation of switch-Statements

In general, the values of the various cases may be far apart:

- generate an if-ladder, that is, a sequence of if-statements
- ullet for n cases, an  $\mathtt{if}$ -cascade (tree of conditionals) can be generated  $\leadsto O(\log n)$  tests
- $\bullet$  if the sequence of numbers has small gaps (  $\leq$  3), a jump table may be smaller and faster
- one could generate several jump tables, one for each sets of consecutive cases
- an if cascade can be re-arranged by using information from profiling, so that paths
  executed more frequently require fewer tests

```
Chapter 4:
Functions
```

### Ingredients of a Function

The definition of a function consists of

- a name with which it can be called;
- a specification of its formal parameters;
- possibly a result type;
- a sequence of statements.

In C we have:

```
\operatorname{code}_{\mathrm{R}}^{i} f \rho = \operatorname{loadc} R_{i} \_f \quad \text{with} \_f \text{ starting address of } f
```

### Observe:

- function names must have an address assigned to them
- since the size of functions is unknown before they are translated, the addresses of forward-declared functions must be inserted later

### Memory Management in Functions

Improvements for Jump Tables

```
int fac(int x) {
    if (x<=0) return 1;
    else return x*fac(x-1);
}

int main (void) {
    int n;
    n = fac(2) + fac(1);
    printf("%d", n);
}</pre>
```

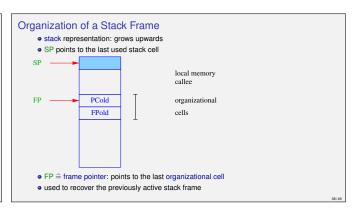
At run-time several instances may be active, that is, the function has been called but has not yet returned.

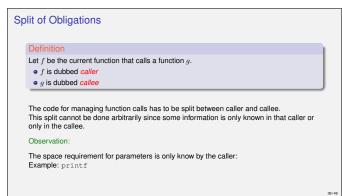
The recursion tree in the example:

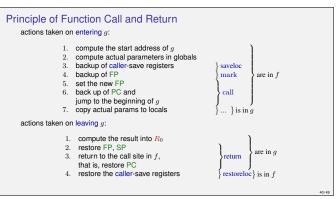


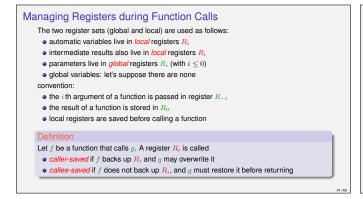
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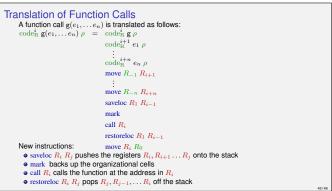
# Memory Management in Function Variables The formal parameters and the local variables of the various instances of a function must be kept separate Idea for implementing functions: • set up a region of memory each time it is called • in sequential programs this memory region can be allocated on the stack • thus, each instance of a function has its own region on the stack • these regions are called stack frames

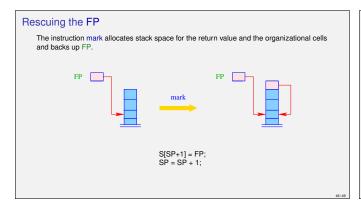


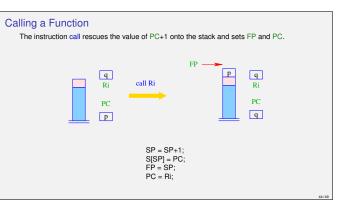


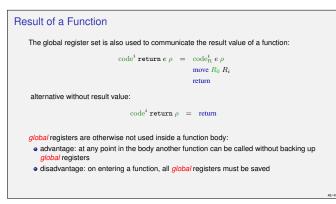


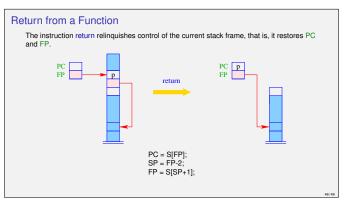












```
Translation of Functions
```

The translation of a function is thus defined as follows:

```
\begin{array}{rcl} \operatorname{code}^1 t_r \ \mathbf{f}(\mathit{args}) \{\mathit{decls} \ \ \mathit{ss} \} \ \rho &=& \operatorname{move} R_{t+1} \ R_{-1} \\ & \vdots \\ & \operatorname{move} R_{t+n} \ R_{-n} \\ & \operatorname{code}^{t+n+1} \ \mathit{ss} \ \rho' \\ & \operatorname{return} \end{array}
```

### Assumptions:

- $\bullet$  the function has n parameters
- ullet the local variables are stored in registers  $R_1, \dots R_l$
- ullet the parameters of the function are in  $R_{-1}, \dots R_{-n}$
- $\bullet$   $\rho'$  is obtained by extending  $\rho$  with the bindings in  $\mathit{decls}$  and the function parameters  $\mathit{args}$
- return is not always necessary

Are the move instructions always necessary?

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Translation of Whole Programs
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A program P=F_1;\dots F_n must have a single main function. {\rm code}^1\ P\ \rho \qquad = \qquad {\rm loadc}\ {\it R}_1\ \_{\rm main}
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 $\begin{array}{c} \rho & = & \text{locate } I_1 \text{ } \\ \text{mark} \\ \text{call } R_1 \\ \text{halt} \\ \text{ } f_1: & \text{code}^1 \ F_1 \ \rho \oplus \rho_{f_1} \\ & \vdots \end{array}$ 

 $\_f_n : \operatorname{code}^1 F_n \rho \oplus \rho_{f_n}$ 

### Assumptions:

- $\bullet \ \rho = \emptyset$  assuming that we have no global variables
- $\bullet$   $\rho_{f_i}$  contain the addresses of the functions up to  $f_i$
- $\bullet \ \rho_1 \oplus \rho_2 = \lambda x \, . \left\{ \begin{array}{ll} \rho_2(x) & \text{if } x \in \mathrm{dom}(\rho_2) \\ \rho_1(x) & \text{otherwise} \end{array} \right.$

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